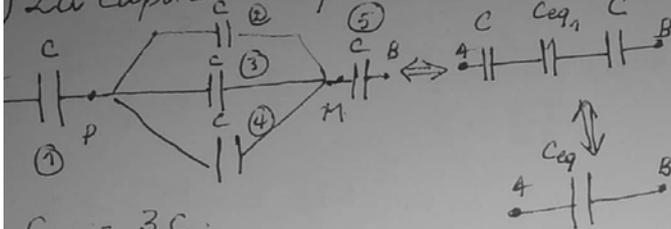


Correction du TD N°03 (électrostatique)

EX 01

on donne  $C = 24 \text{ F}$

La capacité équivalente.



$$C_{eq} = 3C$$

$$\frac{1}{C_{eq}} = \frac{1}{C} + \frac{1}{3C} + \frac{1}{C}$$

$$\frac{1}{C_{eq}} = \frac{7}{3C} \Rightarrow C_{eq} = \frac{3}{7} C$$

$$C_{eq} = \frac{3}{7} \times 24 \text{ F} = 8,57 \times 10^{-5} \text{ F}$$

$$C_{eq} = 8,57 \times 10^{-5} \text{ F}$$

$U_{AB} = 500 \text{ V}$  entre A et B

$$V_{AB} = V_{AP} + V_{PM} + V_{MB}$$

$$\frac{Q}{C_{eq}} = \frac{Q}{C} + \frac{Q}{3C} + \frac{Q}{C}$$

$$U_{AB} = \frac{Q}{C_{eq}} \Rightarrow Q = U_{AB} \cdot C_{eq}$$

$$= 500 \times 8,57 \times 10^{-5}$$

$$Q = 4,28 \times 10^{-4} \text{ C}$$

$$U_{AP} = \frac{Q}{C} = \frac{4,28 \times 10^{-4}}{2 \times 10^{-6}} = 214,28 \text{ V}$$

$$U_{PM} = \frac{Q}{3C} \Rightarrow \frac{4,28 \times 10^{-4}}{3 \times 2 \times 10^{-6}} = 71,42 \text{ V}$$

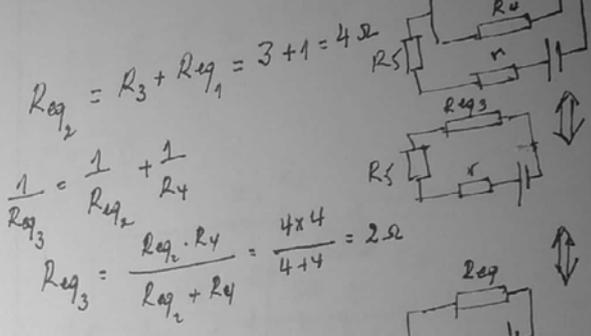
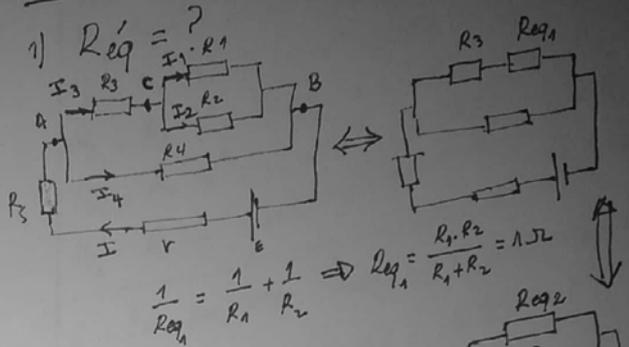
$$U_{MB} = \frac{Q}{C} \Rightarrow \frac{4,28 \times 10^{-4}}{2 \times 10^{-6}} = 214,28 \text{ V}$$

$$Q = 4,28 \times 10^{-4} \text{ C} \quad (C_1)$$

$$Q = 4,28 \times 10^{-4} \text{ C} \quad (C_5)$$

$$Q = 1,42 \times 10^{-4} \text{ C} \quad (C_2, C_3, C_4)$$

EX 02



$R_{eq} = R_{eq3} + R5 + r = 2 + 6 + 1 = 9 \Omega$

$R_{eq} = 9 \Omega$

2) le courant fourni par la source.  
 $E = U_{Req} = R_{eq} \cdot I$

$I = \frac{E}{R_{eq}} = \frac{4,5}{9} = 0,5 \text{ A}$

$I = I4 + I3$   
 $I3 = I1 + I2$

$E = rI + R5I + U_{AB} \Rightarrow U_{AB} = E - rI - R5I$   
 $U_{AB} = 4,5 - 1(0,5) - 6(0,5)$   
 $U_{AB} = 2 \text{ V}$

$U_{AB} = R4 \cdot I4 \Rightarrow I4 = \frac{U_{AB}}{R4} = \frac{2}{4} = 0,25 \text{ A}$

$I3 = I - I4 = 0,5 - 0,25 = 0,25 \text{ A}$   
 $I3 = I4 = 0,25 \text{ A}$

$U_{AB} = 1 \text{ V}$   
 $U_{AB} = R3 \cdot I3 + U_{CB} \Rightarrow U_{CB} = U_{AB} - R3 \cdot I3$

$U_{CB} = 1 - 3 \times (0,25) = 0,25 \text{ V}$

$I3 = I1 + I2$  ( $R1 = R2$ )  
 $I1 = I2$   
 $I3 = 2I1 \Rightarrow I1 = I2 = \frac{I3}{2} = \frac{0,25}{2}$   
 $I1 = I2 = 0,125 \text{ A}$

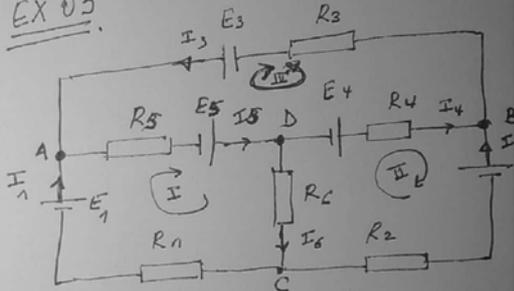
$U_r = r \cdot I = 1 \times 0,5 = 0,5 \text{ V}$   
 $U_{R5} = R5 \cdot I = 6 \times 0,5 = 3 \text{ V}$   
 $U_{R4} = R4 \cdot I4 = 4 \times 0,25 = 1 \text{ V}$   
 $U_{R3} = R3 \cdot I3 = 3 \times 0,25 = 0,75 \text{ V}$   
 $U_{R1} = R1 \cdot I1 = 2 \times 0,125 = 0,25 \text{ V}$   
 $U_{R2} = R2 \cdot I2 = 2 \times 0,125 = 0,25 \text{ V}$

4) L'énergie dissipée par chacune.  
 résistance.

$W_{joule} = \left\{ \begin{matrix} R \cdot I_{eff}^2 \\ ( \Omega ) \quad ( A ) \end{matrix} \right\} \cdot t$   
 ↑  
 énergie dissipée par effet joule (joule)  
 $P_{joule}$   
 ↓ (s)

$P = R I^2 = R \cdot I \cdot I = U \cdot I$

EX 03



Les lois de Kirchhoff  
1<sup>er</sup> loi [loi des nœuds]

noeud A :  
 $I_5 = I_1 + I_3$  --- (1)

noeud B :  
 $I_3 = I_2 + I_4$  --- (2)

noeud C :  
 $I_6 = I_2 + I_1$  --- (3)

noeud D :  
 $I_5 = I_4 + I_6$

2<sup>eme</sup> Loi [loi des mailles]

maille I  
 $R_1 I_1 + R_5 I_5 + R_6 I_6 = E_1 + E_5$  --- (4)

maille II  
 $R_4 I_4 - R_6 I_6 - R_2 I_2 = E_4 - E_2$  --- (5)

maille III  
 $-R_3 I_3 - R_5 I_5 - R_4 I_4 = -E_5 - E_3 - E_4$  --- (6)

on remplace (1), (2) et (3) dans (4), (5) et (6)

$$\begin{cases} 14 I_1 + 10 I_2 + 2 I_3 = 42 \\ -10 I_1 - 16 I_2 + 4 I_3 = -20 \\ -2 I_1 + 4 I_2 - 8 I_3 = -56 \end{cases}$$

$$\Delta = \begin{vmatrix} 14 & 10 & 2 \\ -10 & -16 & 4 \\ -2 & 4 & 8 \end{vmatrix} = \dots$$

$$I_1 = \frac{\Delta_1}{\Delta} = \frac{\begin{vmatrix} 42 & 10 & 2 \\ -20 & -16 & 4 \\ -56 & 4 & 8 \end{vmatrix}}{\Delta} = -2 \text{ A}$$

$$I_2 = \frac{\Delta_2}{\Delta} = \frac{\begin{vmatrix} 14 & 42 & 2 \\ -10 & -20 & 4 \\ -2 & -56 & 8 \end{vmatrix}}{\Delta} = 5 \text{ A}$$

$$I_3 = \frac{\Delta_3}{\Delta} = \frac{\begin{vmatrix} 14 & 10 & 42 \\ -10 & -16 & -20 \\ -2 & 4 & -56 \end{vmatrix}}{\Delta} = 10 \text{ A}$$

$$I_5 = I_1 + I_3 = 8 \text{ A}$$

$$I_4 = I_3 - I_2 = 5 \text{ A}$$

$$I_6 = I_1 + I_2 = 3 \text{ A}$$